

"Teacher"

Name: _____

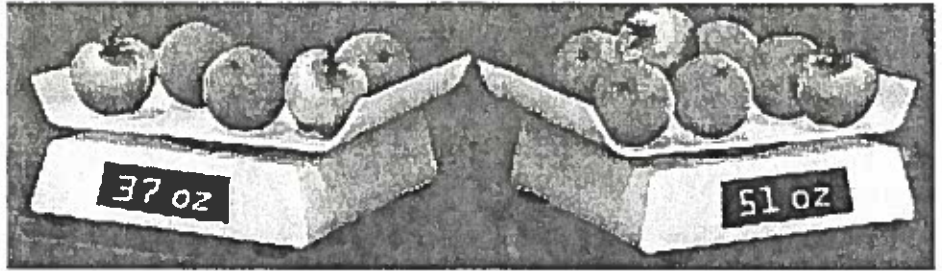
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Section 2S7

Solve Systems by Simple Elimination

A fruit stand sells fresh fruit by the weight. All apples weigh the same and all oranges weigh the same. A customer wants to know - What is the weight of 1 apple? What is the weight of 1 orange? (Hint: Look at what is the same on each scale.)



Discuss with your group. Write down your observations and any calculations you do.

On the first scale there are 2 apples and 3 oranges.
But on the second scale there are still 2 apples and 5 oranges. But on both scales there are (2 apples)
Just different amounts of oranges.

∴ both 2 apples, 3 or (or more)

∴ 3 oranges, 2 apples → 37oz

∴ 5 oranges, 2 apples → 51oz

• 17oz per oranges.

• 8oz per apples.

leftover: 14oz is 2 oranges → $14 \div 2 = 7oz$

$7(5) = 35$ $51 - 35 = 16$ $16 \div 2 = 8$

Oranges

Key Idea:

Just like the real-world situation, we can eliminate in algebraic systems by adding the equations together.

$$\begin{array}{r}
 1) \quad 2x + 5y = 17 \\
 \quad 6x - 5y = -9 \\
 \hline
 8x + 0y = 8 \\
 \quad 8x = 8 \\
 \quad \frac{8}{8} \quad \frac{8}{8} \\
 \quad x = 1
 \end{array}$$

$$\begin{array}{r}
 2x + 5y = 17 \\
 2(1) + 5y = 17 \\
 \quad 2 + 5y = 17 \\
 \quad -2 \quad \quad -2 \\
 \hline
 \quad 5y = 15 \\
 \quad \frac{5}{5} \quad \frac{15}{5} \\
 \quad y = 3
 \end{array}$$

(1, 3)

check BOTH

$$\begin{array}{l}
 2(1) + 5(3) = 17 \\
 2 + 15 = 17 \quad \checkmark
 \end{array}$$

$$\begin{array}{l}
 6(1) - 5(3) = -9 \\
 6 - 15 = -9 \quad \checkmark
 \end{array}$$

Steps

- 1) Add the equations to eliminate one of the variables.
- 2) Solve for the remaining variable.
- 3) Substitute the variable you found back into one of the original equations.
- 4) Solve for the other variable.
- 5) Write the solution as an ordered pair.

$$2) \quad \begin{aligned} 2x + 4y &= 22 \\ -2x + 2y &= 8 \end{aligned}$$

$$\begin{array}{r} 0x + 6y = 36 \\ 6y = 36 \\ \hline 6 \quad 6 \\ y = 6 \end{array}$$

$$2x + 4y = 22$$

$$2x + 4(6) = 22$$

$$2x + 24 = 22$$

$$-24 \quad -24$$

$$\hline 2x = -2$$

$$\hline \frac{2}{2} \quad \frac{-2}{2}$$

$$x = -1$$

$(-1, 6)$

$$3) \quad \begin{aligned} -x + 5y &= 13 \\ x - y &= 15 \end{aligned}$$

$$\begin{array}{r} 4y = 28 \\ \hline 4 \quad 4 \\ y = 7 \end{array}$$

$$-x + 5y = 13$$

$$-x + 5(7) = 13$$

$$-x + 35 = 13$$

$$-35 \quad -35$$

$$\hline -x = -22$$

$$\hline \frac{-x}{-1} = \frac{-22}{-1}$$

$$x = 22$$

$(22, 7)$

$$4) \quad \begin{aligned} x - 3y &= -11 \\ 3x + 3y &= 27 \end{aligned}$$

5) Joseph goes to a store and buys 3 collared shirts and 2 ties. He spends \$80 in total. His brother John buys 4 collared shirts, but he returns 2 ties for a full refund, so he only pays \$60. How much does 1 collared shirt cost? How much does 1 tie cost?

x: cost of 1 collared shirt

y: cost of tie

Joseph: $3x + 2y = 80$

John: $4x - 2y = 60$

$$7x + 0y = 140$$

$$7x = 140$$

$$\hline \frac{7}{7} \quad \frac{140}{7}$$

$$x = 20$$

$$3x + 2y = 80$$

$$3(20) + 2y = 80$$

$$60 + 2y = 80$$

$$-60 \quad -60$$

$$\hline 2y = 20$$

$$\hline \frac{2}{2} \quad \frac{20}{2}$$

$$y = 10$$

The cost of 1 collared shirt is \$20 and the cost of 1 tie is \$10.